

Effects of disoriented chiral condensates on two- and three-pion correlations of relativistic nuclear collisions

Hiroki Nakamura¹ and Ryoichi Seki^{2,3}

¹*Department of Physics, Waseda University, Tokyo 169-8555, Japan*

²*Department of Physics, California State University, Northridge, California 91330*

³*W. K. Kellogg Radiation Laboratory, 106-38, California Institute of Technology, Pasadena, California 91125*

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Two- and three-pion correlations are investigated in cases when a disoriented chiral condensate (DCC) occurs. A chaoticity and weight factor are used as measures of two- and three-pion correlations, and the various models for the DCC are investigated. Some models are found to yield the chaoticity and weight factor in a reasonable agreement with recent experimental data.

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I. INTRODUCTION

It is expected that chiral symmetry will be restored within the high-temperature region generated by high-energy nuclear or proton collisions. The phase transition associated with the restoration may be of a nonequilibrium nature, caused by the rapid expansion and cooling of the high-temperature region. Through such a phase transition, the chiral order parameter could have a direction in the isospin space, different from that in the true vacuum. This phenomenon is called the disoriented chiral condensate (DCC) and has been intensely investigated in the last several years [1]. The most prominent signature of the DCC is expected to be that the fractional neutral-pion number obeys a specific probability distribution, a simple version of which is

$$P(f) = \frac{1}{2\sqrt{f}}, \quad (1)$$

derived by assuming that the direction of condensates is isotropic in the isospin space [1,15]. Here, f is the fractional neutral-pion number, a ratio of the neutral-pion number and the total pion number, given by $f = N_{\pi_0} / (N_{\pi_+} + N_{\pi_-} + N_{\pi_0})$. The distribution predicts a large probability that the number of the neutral pions is observed to be much less than that of the charged pions. Apparently such events, known as Centauro events [2], are observed in cosmic-ray experiments. Accelerator experiments, such as the Minimax and WA98 experiments, have attempted to measure this distribution [3,4], but no clear signature of such a distribution has been observed.

In relativistic heavy-ion collisions, two-pion correlations have been used to obtain information about the size and shape of the pion-emitting source, based on the Hanbury Brown–Twiss (HBT) effect. Three-pion correlations are expected to provide possibly new information about the source [5,6]. The first experimental data regarding the three-pion correlations has been recently reported [7]. In our previous paper [8], we investigated effects of a not completely chaotic source on the two- and three-pion correlations, without referring to any specific dynamics involved in the phase transition. If a DCC should occur, a natural question would be

how well effects of the DCC could be observed in pion interferometry. In this paper, we address that question.

It has been pointed out that the two-pion correlations yield anomalous values when the pions are emitted from a single coherent source exhibiting a DCC [9–12]. Perhaps it is reasonable to assume the pion-emitting source associated with a DCC to be coherent. As we will discuss in Sec. III, the pions emitted from such a source do not exhibit the HBT effect and do not serve as a means of identifying a DCC. It would be naive, however, to assume that the pions would be emitted by a single coherent source exhibiting a DCC and by nothing else. For example, there could be more than one coherent source associated with a DCC, or coherent sources could appear with the background of a chaotic source. It is quite reasonable to expect that such a domain structure might occur at the appearance of a DCC [15,12,1]. We investigate the effects on both the two- and three-pion correlations, of various possible characteristics of a source having domain structure.

A note on terminology. As mentioned above, we treat a source or multiple sources of the DCC as coherent. If a source is not associated with a DCC, we will call it generic. A generic source or generic sources can be either coherent or chaotic. A generic source that is combined with DCC sources will, however, be regarded as chaotic in this work. In our previous work [8], we investigated models in which coherent and chaotic generic sources are combined in various ways. The DCC models in Sec. IV have the same structure as the models in the previous work, except that a DCC source or DCC sources have been replaced by a coherent source or coherent sources, respectively. In figures, we will compare numerical results obtained by the use of the two groups of models. When we do so, we will introduce abbreviated names of the models for clear identification of curves in the figures.

In Sec. II, pion spectra and correlation functions are reviewed, and a chaoticity and weight factor are defined as measures of the strength of two- and three-pion correlations. We investigate correlations for a single DCC domain in Sec. III, and for a more realistic pion source involving a DCC in Sec. IV. In Sec. V, we compare our results with a recent experiment and present a summary of this work.

II. PION SPECTRA AND CORRELATION FUNCTIONS

In this section, for clarity, we define the pion spectra and correlation functions that will be used in the rest of this work. Our definitions are conventional.

One-, two-, and three-pion spectra are given by

$$W_1^i(p) = \langle a_p^{i\dagger} a_p^i \rangle, \quad (2a)$$

$$W_2^{ij}(p_1, p_2) = \langle a_{p_1}^{i\dagger} a_{p_2}^j \dagger a_{p_1}^i a_{p_2}^j \rangle, \quad (2b)$$

$$W_3^{ijk}(p_1, p_2, p_3) = \langle a_{p_1}^{i\dagger} a_{p_2}^j \dagger a_{p_3}^k \dagger a_{p_1}^i a_{p_2}^j a_{p_3}^k \rangle, \quad (2c)$$

where i, j , and k stand for $+$, $-$, or 0 , specifying the pion charge such as π_+ , π_- , or π_0 , respectively. All momenta are on-shell, $p^0 = \sqrt{\mathbf{p}^2 + m^2}$, above and hereafter. $\langle \dots \rangle$ is formally $\langle \psi | \dots | \psi \rangle$ in terms of the quantum state, $|\psi\rangle$, or $\text{Tr}\{\hat{\rho} \dots\}$ in terms of the density matrix, $\hat{\rho}$. In this work we introduce various models in place of the formal definition.

In terms of the spectra, we define correlation functions as

$$C_2^{ij}(p_1, p_2) = \frac{W_2^{ij}(p_1, p_2)}{W_1^i(p_1)W_1^j(p_2)}, \quad (3a)$$

$$C_3^{ijk}(p_1, p_2, p_3) = \frac{W_3^{ijk}(p_1, p_2, p_3)}{W_1^i(p_1)W_1^j(p_2)W_1^k(p_3)}. \quad (3b)$$

As in [13], in order to exclude the effect of multiplicity fluctuation, we use normalized correlation functions for identical pions:

$$\bar{C}_2^{ii}(p_1, p_2) = \frac{\langle \hat{n}_i \rangle^2}{\langle \hat{n}_i(\hat{n}_i - 1) \rangle} C_2^{ii}(p_1, p_2), \quad (4a)$$

$$\bar{C}_3^{iii}(p_1, p_2, p_3) = \frac{\langle \hat{n}_i \rangle^3}{\langle \hat{n}_i(\hat{n}_i - 1)(\hat{n}_i - 2) \rangle} C_3^{iii}(p_1, p_2, p_3), \quad (4b)$$

where

$$\langle \hat{n}_i \rangle = \int d^3p W_1^i(p), \quad (5a)$$

$$\langle \hat{n}_i(\hat{n}_i - 1) \rangle = \int d^3p_1 d^3p_2 W_2^{ii}(p_1, p_2), \quad (5b)$$

$$\langle \hat{n}_i(\hat{n}_i - 1)(\hat{n}_i - 2) \rangle = \int d^3p_1 d^3p_2 d^3p_3 W_3^{iii}(p_1, p_2, p_3). \quad (5c)$$

Here, \hat{n}_i is the number operator, $\hat{n}_i = \int d^3p a_p^{i\dagger} a_p^i$.

We define chaoticity, $\lambda_{ij}(p)$, and weight factor, $\omega_{ijk}(p)$, as

$$\lambda_{ij}(p) = (\bar{C}_2^{ij}(p_1, p_2) - 1)_{p_1=p_2=p}, \quad (6)$$

$$\omega_{ijk}(p) = \frac{\bar{C}_3^{ijk}(p_1, p_2, p_3) - 1 - (\bar{C}_2^{ij}(p_1, p_2) + \bar{C}_2^{jk}(p_2, p_3) + \bar{C}_2^{ki}(p_3, p_1) - 3)}{2 \sqrt{(\bar{C}_2^{ij}(p_1, p_2) - 1)(\bar{C}_2^{jk}(p_2, p_3) - 1)(\bar{C}_2^{ki}(p_3, p_1) - 1)}} \Bigg|_{p_1=p_2=p_3=p}. \quad (7)$$

$\lambda_{ij}(p)$ and $\omega_{ijk}(p)$ are measures of the strength of the two- and three-pion correlations. Note that λ_{ij} and ω_{ijk} are defined for zero relative momenta. ω_{ijk} has been extracted from the recent experiment for small relative momenta [7], but the difference is immaterial since it is a slowly varying function of the relative momenta [5,6]. When $\lambda_{ij}(p)$ is unity or zero, we call the pion-emitting source chaotic or coherent, respectively. For a chaotic source, $\omega_{ijk}(p)$ of identical particles is unity.

III. A SINGLE COHERENT SOURCE ASSOCIATED WITH DCC

In this section, we examine the case of pions that are emitted from a single coherent source associated with a DCC. The correlation functions in this case can be derived in two different ways, by the isosinglet method and by the generating functional method. The isosinglet method has been previously used to obtain the anomalous values of the two-pion correlation functions [14]. The generating functional

method [15] is a more systematic approach, and we will apply it to more complicated cases in Sec. IV. Though the two methods yield the same result in this simple case, we will show both for the sake of comparison. These methods are not different essentially from preceding calculation in [10]. Both methods show that no HBT effect occurs in this case.

A. Isosinglet method

An isosinglet state vector of $2N$ pions is given by

$$|\psi\rangle = \frac{1}{\sqrt{(2N+1)!}} I^{\dagger N} |0\rangle, \quad (8)$$

where

$$I = 2a_+ a_- - a_0^2. \quad (9)$$

I is an isosinglet operator [16,14,9]. Since the creation and annihilation operators are of a single mode, the momentum variables are not explicitly shown here. The probability of finding $2n$ neutral pions is

$$P_{2n,2N} = \frac{(N!)^2 2^{2N} (2n)!}{(2N+1)! (n!)^2 2^{2n}} \rightarrow \frac{1}{2\sqrt{n/N}} \quad (N, n \gg 1). \quad (10)$$

This large N and n limit is consistent with Eq. (1). The positive-pion spectra come out to be [10]

$$W_1^+ = \frac{2}{3}N, \quad (11a)$$

$$W_2^{++} = \frac{8}{15}N(N-1), \quad (11b)$$

$$W_3^{+++} = \frac{16}{35}N(N-1)(N-2). \quad (11c)$$

In the large- N limit, the two- and three-pion correlations for various combinations of pion charges defined in Eqs. (3) are then

$$C_2^{\pm\pm} = C_2^{\pm\mp} = \frac{6}{5}, \quad (12a)$$

$$C_2^{\pm 0} = \frac{4}{5}, \quad (12b)$$

$$C_2^{00} = \frac{9}{5}, \quad (12c)$$

$$C_3^{\pm\pm\pm} = C_3^{\pm\pm\mp} = \frac{54}{35}, \quad (12d)$$

$$C_3^{\pm\pm 0} = C_3^{\pm\mp 0} = \frac{54}{105}, \quad (12e)$$

$$C_3^{\pm 00} = \frac{27}{35}, \quad (12f)$$

$$C_3^{000} = \frac{27}{7}. \quad (12g)$$

The anomalous values of the two-pion correlations, Eqs. (12a)–(12c), agree with those given previously [9]. We see that the three-pion correlation functions also yield anomalous values.

The DCC gives correlation functions different from those of a coherent generic source. We note, however, that the normalized correlation functions, \bar{C} 's, are the same as those of a coherent generic source, all being unity. The reason for this is seen as follows: The isosinglet method is applied for a single mode (momentum), and yields the same W 's for all modes. The normalization condition, Eq. (5), thus guarantees

that all \bar{C} 's as defined in Eq. (4) are unity, the same value as those of the coherent generic source. The pions emitted from a single coherent DCC source do not then exhibit the HBT effect and do not serve as a means of identifying a DCC.

B. Generating functional method

In order to achieve the isosinglet property of a DCC, pion spectra should be averaged over all directions of isospin space [15]. We evaluate correlation functions with c -number source-current formalism.

In c -number source-current formalism, a generating functional method is useful [17]. We define the generating functional (slightly differently from [17]) as

$$G[z_i^*(p), z_i(p)] = \left\langle \exp \left\{ \sum_i \int \frac{d^3p}{\sqrt{(2\pi)^3} \cdot 2p^0} [z_i^*(p) J_i^*(p) + z_i(p) J_i(p)] \right\} \right\rangle_J, \quad (13)$$

where $J_i(p)$ is the c -number source current for the pion charge, $i = +, -, \text{ or } 0$. $\langle \dots \rangle_J$ is the statistical average of the fluctuation of $J_i(p)$. Using this generating functional, we can obtain

$$\begin{aligned} & \langle a_{p_1}^{i_1 \dagger} a_{p_2}^{i_2 \dagger} \dots a_{p_n}^{i_n \dagger} a_{q_1}^{j_1} a_{q_2}^{j_2} \dots a_{q_m}^{j_m} \rangle \\ &= \frac{\delta^{n+m} G[z_i^*(p), z_i(p)]}{\delta z_{i_1}^*(p_1) \dots \delta z_{i_n}^*(p_n) \delta z_{j_1}(q_1) \dots \delta z_{j_m}(q_m)} \Bigg|_{z_i(p)=0}. \end{aligned} \quad (14)$$

Following [15], we set the source current of each kind of pion, $J_i(p)$, as

$$J_0(p) = J(p) n_3, \quad (15)$$

$$J_{\pm}(p) = J(p) \frac{n_1 \mp i n_2}{\sqrt{2}}, \quad (16)$$

where \mathbf{n} is a unit vector in isospin space. The ratio of neutral pions, f , is given by

$$f = n_3^2, \quad (17)$$

and $|n_{\pm}|^2 = (1-f)/2$. n_i is independent of momentum because we assume that all modes of momenta condense in the same direction in isospin space. Due to the isotropic distribution of the unit vector, the average that appears in Eq. (13) becomes

$$\langle \dots \rangle_J = \int \frac{d^3\mathbf{n}}{4\pi} \delta(|\mathbf{n}|-1) \dots. \quad (18)$$

When we treat identical pions, the integrand of the right-hand side depends on only n_3^2 or $|n_{\pm}|^2$. In such cases, we can replace the integral as

$$\int \frac{d^3\mathbf{n}}{4\pi} \delta(|\mathbf{n}|-1) \cdots = \int_0^1 df P(f) \cdots, \quad (19)$$

where $P(f)$ is defined in Eq. (1).

The neutral-pion spectrum for the DCC is obtained as

$$\begin{aligned} W_1^0(p) &= \int_0^1 P(f) df n_3^2 W(p) \\ &= \frac{1}{3} W(p), \end{aligned} \quad (20)$$

where

$$W(p) = \frac{1}{2p^0(2\pi)^3} |J(p)|^2. \quad (21)$$

For the charged pions, we obtain

$$W_1^\pm(p) = W_1^0(p). \quad (22)$$

Similarly, we can derive the two-pion spectra,

$$W_2^{\pm\pm}(p_1, p_2) = W_2^{\pm\mp}(p_1, p_2) = \frac{2}{15} W(p_1) W(p_2), \quad (23a)$$

$$W_2^{0\pm}(p_1, p_2) = \frac{1}{15} W(p_1) W(p_2), \quad (23b)$$

$$W_2^{00}(p_1, p_2) = \frac{1}{5} W(p_1) W(p_2). \quad (23c)$$

Three-pion spectra are

$$\begin{aligned} W_3^{\pm\pm\pm}(p_1, p_2, p_3) &= W_3^{\pm\pm\mp}(p_1, p_2, p_3) \\ &= \frac{2}{35} W(p_1) W(p_2) W(p_3), \end{aligned} \quad (24a)$$

$$\begin{aligned} W_3^{\pm\pm 0}(p_1, p_2, p_3) &= W_3^{\pm\mp 0}(p_1, p_2, p_3) \\ &= \frac{2}{105} W(p_1) W(p_2) W(p_3), \end{aligned} \quad (24b)$$

$$W_3^{\pm 00}(p_1, p_2, p_3) = \frac{1}{35} W(p_1) W(p_2) W(p_3), \quad (24c)$$

$$W_3^{000}(p_1, p_2, p_3) = \frac{1}{7} W(p_1) W(p_2) W(p_3). \quad (24d)$$

Equations (23) and (24) yield the same correlation functions as those obtained by the use of the isosinglet method, Eqs. (12) [10]. Furthermore, $W(p)$ of Eq. (21) corresponds to the pion-number density for the mode (momentum) p , and W_n 's are n products of $W(p)$'s. Accordingly, when the normalization condition of Eq. (5) is imposed, the \bar{C} 's automatically become unity, which is the same value of \bar{C} 's as in the co-

herent generic case. We thus see that though the correlation functions are momentum dependent in this method, while they are independent in the isosinglet method, both methods yield the same C 's and also \bar{C} 's = 1.

When the pions are emitted from more than one coherent source with a DCC, or they are also emitted from a chaotic generic source, the HBT effect appears and a DCC could be identified. We will discuss these cases in the following section.

IV. A SOURCE WITH A DCC DOMAIN

In relativistic heavy-ion collisions, it would not be realistic to consider all the pions being emitted from one large DCC source, as in the model in the previous section. In this section, we investigate three models that we expect to be more realistic. In the first model, the source consists of one DCC source and one chaotic generic source, which is performed in [10]. In the second model the source consists of multiple DCC domains. The third model is a combination of the previous two models, multiple DCC domains with one chaotic generic source. The HBT effect appears in these models and helps in identifying the DCC signature in the pion interferometry.

A. A Partially coherent DCC source (PC-DCC)

In this subsection, we introduce a partially coherent (PC) source with a DCC [15,12]. This model is the same as previously treated in [10]. Source current, $J_i(p)$, is separated into two parts as

$$J_i(p) = J_D(p) n_i + J_g^i(p), \quad (25)$$

where $J_D(p)$ is the DCC source current and $J_g^i(p)$ is the generic one. We assume that the DCC source is coherent and that the generic source is chaotic. The average in Eq. (13) becomes

$$\begin{aligned} \langle \cdots \rangle_J &= \int \frac{d^3\mathbf{n}}{4\pi} \delta(|\mathbf{n}|-1) \int \cdots \prod_{i=1}^3 \mathcal{P}_i[J_g^{i*}(p), J_g^i(p)] \\ &\quad \times \mathcal{D}J_g^i(p) \mathcal{D}J_g^{i*}(p), \end{aligned} \quad (26)$$

where $\mathcal{P}_i[J_g^{i*}(p), J_g^i(p)]$ is a distribution functional of $J_g^i(p)$ and assumed to have a Gaussian form, as in Ref. [17], so that the higher-order moment of $J_g^i(p)$ is represented by the second-order moment, for example,

$$\begin{aligned} &\langle J_g^{i*}(p_1) J_g^{i*}(p_2) J_g^i(p_1) J_g^i(p_2) \rangle_J \\ &= \langle J_g^{i*}(p_1) J_g^i(p_1) \rangle_J \langle J_g^{i*}(p_2) J_g^i(p_2) \rangle_J \\ &\quad + \langle J_g^{i*}(p_1) J_g^i(p_2) \rangle_J \langle J_g^{i*}(p_2) J_g^i(p_1) \rangle_J. \end{aligned} \quad (27)$$

At first, we concentrate on the case of positive pions. We introduce here several real functions, f_{ij} , ϕ_{ij} , F_{ij}^+ , and Φ_{ij}^+ . These functions are defined as follows [5]:

$$f_{ij} \exp(i\phi_{ij}) \equiv \frac{1}{(2\pi)^3 \sqrt{2p_1^0 \cdot 2p_2^0}} J_D^*(p_i) J_D(p_j), \quad (28)$$

$$F_{ij}^+ \exp(i\Phi_{ij}^+) \equiv \frac{1}{(2\pi)^3 \sqrt{2p_1^0 \cdot 2p_2^0}} \langle J_g^{+*}(p_i) J_g^+(p_j) \rangle_{J_g^+}, \quad (29)$$

where

$$\langle \dots \rangle_{J_g^+} = \int \dots \mathcal{P}_+ [J_g^{+*}(p), J_g^+(p)] \mathcal{D}J_g^+(p) \mathcal{D}J_g^{+*}(p). \quad (30)$$

Hereafter, for simplicity, we denote F_{ij}^+ as F_{ij} . We obtain the positive-pion spectrum,

$$W_1^+(p_1) = \int_0^1 df P(f) W_f^+(p_1) = \frac{1}{3} f_{11} + F_{11}, \quad (31)$$

where

$$W_f^i(p_1) = |n_i|^2 f_{11} + F_{11}^i. \quad (32)$$

The two-pion spectrum is given by

$$\begin{aligned} W_2^+(p_1, p_2) &= \int_0^1 P(f) df \{ W_f^+(p_1) W_f^+(p_2) + R_f^+(p_2, p_3) \} \\ &= \frac{1}{45} f_{11} f_{22} + W_1^+(p_1) W_1^+(p_2) + R^+(p_1, p_2), \end{aligned} \quad (33)$$

where

$$R_f^i(p_1, p_2) = F_{12}^{i2} + 2|n_i|^2 f_{12} F_{12}^i \cos(\Phi_{12} - \phi_{12}), \quad (34)$$

$$R^i(p_1, p_2) = F_{12}^{i2} + \frac{2}{3} f_{12} F_{12}^i \cos(\Phi_{12} - \phi_{12}). \quad (35)$$

The first term in the right-hand side of Eq. (33) does not appear in the case of the partially coherent generic source [8], signifying the new aspect in the partially coherent DCC case. The two-pion correlation function becomes

$$\begin{aligned} C_2^{++}(p_1, p_2) &= 1 + \frac{1}{5} [1 - \epsilon(p_1)][1 - \epsilon(p_2)] \\ &\quad + \frac{R^+(p_1, p_2)}{W_1^+(p_1) W_1^+(p_2)}, \end{aligned} \quad (36)$$

where $\epsilon(p)$ is the ratio of the generic pion number and the total pion number:

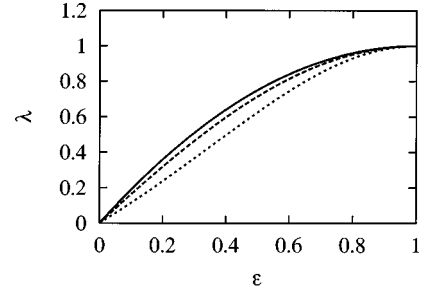


FIG. 1. Chaoticity λ as a function of the ratio of the generic pion number and the total pion number ϵ . The solid curve represents the partially coherent generic model (PC-G). The dashed and dotted curves represent the partially coherent DCC model (PC-DCC) for the positive pions and for the neutral pions, respectively.

$$\epsilon(p_1) = \frac{F_{11}}{\frac{1}{3} f_{11} + F_{11}}. \quad (37)$$

In this case, the normalization of Eq. (4a) is not unity in the limit of the infinite relative momenta. This is because the term $\frac{1}{5} [1 - \epsilon(p_1)][1 - \epsilon(p_2)]$ is momentum dependent. In the following, we proceed by neglecting the momentum dependence of $\epsilon(p)$, so that the correlation function is normalized as in Eq. (4a):

$$\bar{C}_2^{++}(p_1, p_2) = 1 + \frac{1}{1 + \frac{1}{5}(1 - \epsilon)^2} \frac{R^+(p_1, p_2)}{W_1^+(p_1) W_1^+(p_2)}. \quad (38)$$

The chaoticity for normalized correlation function, Eq. (6), is

$$\lambda_{++} = \frac{\epsilon(2 - \epsilon)}{1 + \frac{1}{5}(1 - \epsilon)^2}. \quad (39)$$

This chaoticity is different from that of a partially coherent generic source:

$$\lambda_{generic} = \epsilon(2 - \epsilon), \quad (40)$$

which is evaluated in [5]. In Fig. 1, we show the chaoticity as a function of the ratio, ϵ , for a partially coherent DCC source (PC-DCC). For comparison, we also show in the figure the chaoticity for a partially coherent generic source (PC-G) that has been previously investigated [8,5,13].

The three-pion spectrum is evaluated as

$$\begin{aligned}
W_3^{+++}(p_1, p_2, p_3) &= \int_0^1 df P(f) \left\{ W_f^+(p_1) W_f^+(p_2) W_f^+(p_3) + \sum_{(a,b,c)} W_f^+(p_a) R_f^+(p_b, p_c) \right. \\
&\quad \left. + 2 \left[F_{12} F_{23} F_{31} \cos(\Phi_{12} + \Phi_{23} + \Phi_{31}) + \frac{1-f}{2} \sum_{(a,b,c)} f_{ab} F_{bc} F_{ca} \cos(\phi_{ab} + \Phi_{bc} + \Phi_{ca}) \right] \right\} \\
&= W_1^+(p_1) W_1^+(p_2) W_1^+(p_3) + \sum_{(a,b,c)} W_1^+(p_a) R^+(p_b, p_c) + 2 \left[F_{12} F_{23} F_{31} \cos(\Phi_{12} + \Phi_{23} + \Phi_{31}) \right. \\
&\quad \left. + \frac{1}{3} \sum_{(a,b,c)} f_{ab} F_{bc} F_{ca} \cos(\phi_{ab} + \Phi_{bc} + \Phi_{ca}) \right] + \frac{19}{945} f_{11} f_{22} f_{33} + \frac{1}{45} \sum_{(a,b,c)} f_{aa} f_{bb} F_{cc} \\
&\quad + \frac{2}{45} \sum_{(a,b,c)} f_{aa} f_{bc} F_{bc} \cos(\Phi_{bc} - \phi_{bc}). \tag{41}
\end{aligned}$$

The weight factor for normalized three-pion correlation functions is

$$\begin{aligned}
\omega_{+++} &= \left[\frac{3\epsilon(2-\epsilon) + 2\epsilon^2(3-2\epsilon) + \frac{6}{5}\epsilon(1-\epsilon)^2}{1 + \frac{19}{35}(1-\epsilon)^3 + \frac{3}{5}(1-\epsilon)^2\epsilon} \right. \\
&\quad \left. - 3\lambda_{++} \right] \frac{\lambda_{++}^{-3/2}}{2}. \tag{42}
\end{aligned}$$

Figure 2 illustrates the weight factors for a partially coherent DCC source and a partially coherent generic source as functions of ϵ . The weight factor of a partially coherent DCC model becomes negative for small ϵ . This is the aspect of the DCC case that characteristically differs from the generic case:

$$\omega_{generic} = \sqrt{\epsilon} \frac{3-2\epsilon}{(2-\epsilon)^{3/2}}, \tag{43}$$

which is always positive.

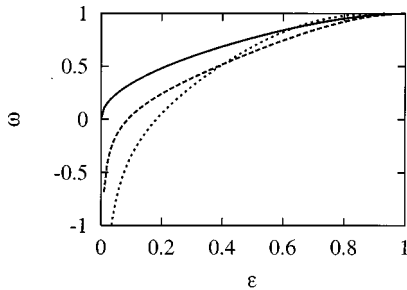


FIG. 2. Weight factor ω as a function of the ratio of the generic pion number and the total pion number ϵ . The solid curve represents the partially coherent generic model (PC-G). The dashed and dotted curves represent the partially coherent DCC model (PC-DCC) for the positive pions and for the neutral pions, respectively.

The chaoticity and weight factor for normalized neutral-pion correlations are

$$\lambda_{00} = \frac{\epsilon(2-\epsilon)}{1 + \frac{4}{5}(1-\epsilon)}, \tag{44}$$

$$\begin{aligned}
\omega_{000} &= \left[\frac{3\epsilon(2-\epsilon) + 2\epsilon^2(3-2\epsilon) + \frac{24}{5}\epsilon(1-\epsilon)^2}{1 + \frac{20}{7}(1-\epsilon)^3 + \frac{12}{5}(1-\epsilon)^2\epsilon} \right. \\
&\quad \left. - 3\lambda_{00} \right] \frac{\lambda_{00}^{-3/2}}{2}. \tag{45}
\end{aligned}$$

These are shown as functions of ϵ in Figs. 1 and 2. The chaoticity for the normalized correlations of differently charged pions vanishes, because the generic part exhibits no HBT effect and the DCC part is taken to be coherent.

It should be noted that the distribution function of the fractional neutral-pion number in the partially coherent DCC model is different from Eq. (1). The fractional neutron-pion number in the partially coherent DCC model is

$$\begin{aligned}
f' &= \frac{W_f^0(p_1)}{W_f^+(p_1) + W_f^-(p_1) + W_f^0(p_1)} \\
&= \frac{f \cdot f_{11} + F_{11}}{f_{11} + 3F_{11}} = f(1-\epsilon) + \frac{1}{3}\epsilon, \tag{46}
\end{aligned}$$

where each kind of pion emitted from the generic source is assumed to have the same multiplicity, or $F_{11}^0 = F_{11}^+ = F_{11}^-$. ϵ is that of Eq. (37). The new probability distribution function for f' , $P'(f')$ is obtained by the use of $P(f)df = P'(f')df'$ as

$$P'(f') = \begin{cases} \frac{1}{2\sqrt{\left(f' - \frac{1}{3}\epsilon\right)(1-\epsilon)}} & \left(\frac{1}{3}\epsilon < f' < 1 - \frac{2}{3}\epsilon\right), \\ 0, & \text{otherwise.} \end{cases} \quad (47)$$

This distribution function becomes Eq. (1) when $\epsilon=0$, or one DCC source with no chaotic source. When $\epsilon=1$, or no DCC source, $P'(f')$ is meaningful only at $f'=\frac{1}{3}$. The charge fluctuation caused by DCC is reduced as the generic source increases.

B. Multiple DCC domains (M-DCC)

In actual experiments, we expect that the DCC would appear not simply in a possibly large, unified area but in several, separated domains. In order to describe such a domain structure, we use multiple coherent sources whose number obeys the Poisson distribution.

In an analogy to the description of a generic source in [13], we write the source current for N DCC domains as

$$J_i(p) = \sum_{n=1}^N j(p) e^{ip \cdot X_n - i\theta_n n_{n,i}}, \quad (48)$$

where $n_{n,i}$ is a unit vector in isospin space, describing the direction of condensate in the n th domain. The position of the n th domain is X_n , distributed according to the function, $\rho(X_n)$. The normalization of $\rho(x)$ is $\int \rho(x) dx = 1$. θ_n is a random number uniformly distributed between 0 and 2π , so as to satisfy the chaotic property among the different domains. N obeys the Poisson distribution, but the zero-domain event, or $N=0$, should be excluded from it. Instead of the usual Poisson distribution, the appropriately renormalized Poisson distribution is then

$$\gamma_N^{(renorm)} = \frac{\alpha^N}{N!} \frac{1}{e^\alpha - 1} \quad \text{for } N=1 \sim \infty. \quad (49)$$

In this case, the average of the generating functional, Eq. (13), is

$$\begin{aligned} \langle \dots \rangle_J &= \sum_{N=1}^{\infty} \gamma_N^{(renorm)} \int \left(\prod_{n=1}^N \frac{d^3 \mathbf{n}_n}{4\pi} \delta(|\mathbf{n}_n| - 1) \right) \\ &\times \int \left(\prod_{n=1}^N dX_N \rho(X_N) \right) \int_0^{2\pi} \left(\prod_{n=1}^N \frac{d\theta_n}{2\pi} \right) \dots \end{aligned} \quad (50)$$

The pion spectra are obtained as

$$W_1^+(p_1) = \frac{\alpha}{3} \frac{|j(p_1)|^2}{1 - e^{-\alpha}}, \quad (51a)$$

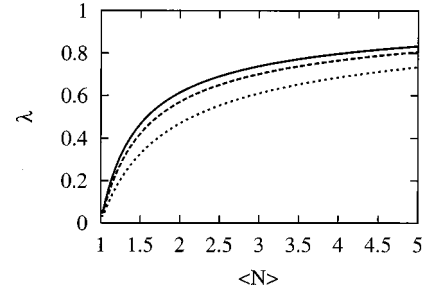


FIG. 3. Chaoticity λ as a function of the mean number of domains $\langle N \rangle$. The solid curve represents the multiple coherent generic sources (M-G). The dashed and dotted curves represent the multiple DCC domain model (M-DCC) for the positive pions and for the neutral pions, respectively.

$$W_2^{++}(p_1, p_2) = \frac{|j(p_1)|^2 |j(p_2)|^2}{1 - e^{-\alpha}} \left[\frac{2}{15} \alpha + \frac{1}{9} \alpha^2 + \frac{1}{9} \alpha^2 |\rho_{12}|^2 \right], \quad (51b)$$

$$\begin{aligned} W_3^{+++}(p_1, p_2, p_3) &= \frac{|j(p_1)|^2 |j(p_2)|^2 |j(p_3)|^2}{1 - e^{-\alpha}} \\ &\times \left[\frac{2}{35} \alpha + \frac{2}{15} \alpha^2 + \frac{1}{27} \alpha^3 \right. \\ &+ \left. \left(\frac{4}{45} \alpha^2 + \frac{1}{27} \alpha^3 \right) \sum_{(a,b)} |\rho_{ab}|^2 \right. \\ &+ \left. \frac{1}{27} \alpha^3 \cdot 2 \operatorname{Re}(\rho_{12} \rho_{23} \rho_{31}) \right], \quad (51c) \end{aligned}$$

where

$$\rho_{ij} = \int d^4 x \rho(x) e^{-i(p_i - p_j) \cdot x}. \quad (52)$$

Using the above equations, we derive the chaoticity and weight factor for normalized correlations as

$$\lambda_{++} = \frac{\alpha}{\alpha + \frac{6}{5}}, \quad (53)$$

$$\omega_{+++} = \frac{\alpha^2 + \frac{6}{5} \alpha + \frac{351}{175} \sqrt{\frac{\alpha + \frac{6}{5}}{\alpha}}}{\alpha^2 + \frac{18}{5} \alpha + \frac{54}{35}}. \quad (54)$$

If the domains are not DCC sources but coherent generic sources, the chaoticity and weight factor become [8]

$$\lambda_{generic} = \frac{\alpha}{\alpha + 1}, \quad (55)$$

$$\omega_{generic} = \frac{1}{2} \frac{2\alpha^2 + 2\alpha + 3}{\alpha^2 + 3\alpha + 1} \sqrt{\frac{\alpha + 1}{\alpha}}, \quad (56)$$

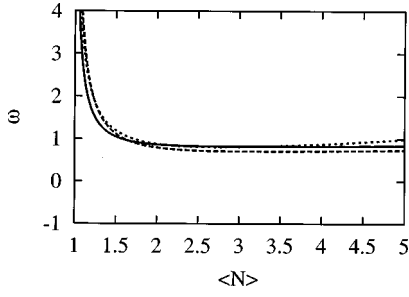


FIG. 4. Weight factor ω as a function of the mean number of domains $\langle N \rangle$. The solid curve represents the multiple coherent generic sources (M-G). The dashed and dotted curves represent the multiple DCC domain model (M-DCC) for the positive pions and for the neutral pions, respectively.

respectively. In Figs. 3 and 4, we show the chaoticity and weight factor of the multiple DCC model (M-DCC) as functions of the mean number of the DCC domains, $\langle N \rangle = \alpha/[1 - \exp(-\alpha)]$. For comparison, we also show in the figure the chaoticity and weight factor of the multiple coherent generic model (M-G) [13] that we examined in our previous work [8].

In this model, the correlations of differently charged pions has no HBT effect. For example, the two-pion correlation function of a paired positive pion and negative pion is

$$W_2^{+-}(p_1, p_2) = \frac{|j(p_1)|^2 |j(p_2)|^2}{1 - e^{-\alpha}} \left[\frac{2}{15} \alpha + \frac{1}{9} \alpha^2 \right]. \quad (57)$$

$W_2^{+-}(p_1, p_2)$ is independent of ρ_{12} . Note that $n_{n,+}^2$ appears during the calculation, but it is reduced to no contribution after averaging over the azimuthal angle by taking account of the isotropic distribution of condensate:

$$\int_0^1 P(f) df \int_0^{2\pi} \frac{d\phi}{2\pi} n_+^2 = \int \frac{1-f}{2} P(f) df \int \exp(2i\phi) \frac{d\phi}{2\pi} = 0, \quad (58)$$

where $n_1 = \sqrt{1-f} \cos \phi$, $n_2 = \sqrt{1-f} \sin \phi$. The HBT effect thus vanishes for a paired positive pion and negative pion by this averaging. Similarly, the correlation of a neutral pion and a charged pion shows no HBT effect.

The chaoticity and weight factor of neutral pions are

$$\lambda_{00} = \frac{\alpha}{\alpha + \frac{9}{5}}, \quad (59)$$

$$\omega_{000} = \frac{1}{2} \frac{2\alpha^2 + \frac{18}{5}\alpha + \frac{1377}{175}}{\alpha^2 + \frac{27}{5}\alpha + \frac{27}{7}} \sqrt{\frac{9}{\alpha + \frac{9}{5}}}. \quad (60)$$

These are illustrated as functions of the mean number of domains in Figs. 3 and 4.

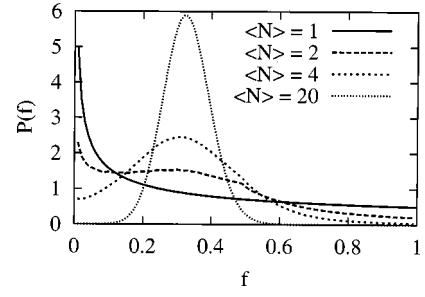


FIG. 5. Probability distributions in the multiple DCC domain model, $P_\alpha(f)$, as a function of the fractional neutral-pion number f the mean domain number, $\langle N \rangle = 1, 2, 4, 20$, (corresponding to $\alpha = 0, 1.59, 3.92, 20.0$, respectively).

As in the case of the partially coherent DCC of the previous subsection, the fractional pion number is also modified in the case of multiple DCC domains. We can write the probability distribution of f for N DCC domains as

$$P_N(f) = \int_0^1 \delta\left(f - \frac{1}{N} \sum_{n=1}^N f_n\right) \times \frac{1}{2\sqrt{f_1}} \cdots \frac{1}{2\sqrt{f_N}} df_1 df_2 \cdots df_N, \quad (61)$$

where f_n is the ratio of the neutral pion number and the total pion number in the n th domain. The pion spectra emitted from each domain is assumed to be the same. The observed distribution is obtained by averaging the above probability distribution with the Poisson distribution, Eq. (49),

$$P_\alpha(f) = \sum_{N=1}^{\infty} \frac{\alpha^N}{N!} \frac{1}{e^{\alpha-1}} P_N(f). \quad (62)$$

Figure 5 illustrates $P_\alpha(f)$ for the mean number of the domains, $\langle N \rangle = 1, 2, 4$, and 20. $\langle N \rangle = 1$ corresponds to Eq. (1). Figure 5 is similar to a figure in [12], where no detail of the derivation is given. The distribution indeed becomes sharper as $\langle N \rangle$ increases [12,1].

C. Multiple DCC domains with a chaotic generic source (M-DCC/G)

We now consider the case of multiple DCC domains with one chaotic source emitting generic pions. This model corresponds to the combination of the two models in the previous subsections. Note that the Poisson distribution used in the current model is the usual one, instead of Eq. (49):

$$\gamma_N^{(usual)} = \frac{\alpha^N}{N!} e^{-\alpha}. \quad (63)$$

The source current is

$$J_i(p) = \sum_{n=1}^N j(p) e^{ip \cdot X_n - i\theta_n n_{n,i}} + J_g^i(p), \quad (64)$$

where the variables are defined in the same way as in the previous subsections. For convenience, we introduce S_{ab}^i and T_{ab} :

$$T_{ab} = \frac{j^*(p_a)j(p_b)}{2(2\pi)^3 \sqrt{p_a^0 p_b^0}} \rho_{ab}, \quad (65)$$

$$S_{ab}^i = \frac{1}{2(2\pi)^3 \sqrt{p_a^0 p_b^0}} \langle J_g^{i*}(p_a) J_g^i(p_b) \rangle_{J_g^i}, \quad (66)$$

where ρ_{ij} is defined in Eq. (52) and S_{ab}^i is equivalent to $F_{ab}^i \exp(i\Phi_{ab}^i)$ in Eq. (29). Hereafter, when we do not denote the superscript i explicitly, we imply that $+$ is excluded.

The one-pion spectrum and two- and three-pion correlations are

$$W_1^+(p_1) = \frac{\alpha}{3} T_{11} + S_{11}, \quad (67a)$$

$$C_2^{++}(p_1, p_2) = 1 + \frac{\left| \frac{\alpha}{3} T_{12} + S_{12} \right|^2}{1 + \frac{6}{5} \frac{(1-\epsilon)^2}{\alpha}} W_1^+(p_1) W_1^+(p_2), \quad (67b)$$

$$C_3^{+++}(p_1, p_2, p_3) = 1 + \frac{1}{1 + \frac{54}{35} \frac{(1-\epsilon)^3}{\alpha^2} + \frac{18}{5} \frac{(1-\epsilon)^2}{\alpha}} \left\{ \sum_{(a,b)} \frac{\left| \frac{\alpha}{3} T_{ab} + S_{ab} \right|^2 + \frac{4}{15} \alpha(1-\epsilon) |T_{ab}|^2 + \frac{2}{5} (1-\epsilon) \cdot 2 \operatorname{Re}(T_{ab} S_{ba})}{W_1^+(p_a) W_1^+(p_b)} \right. \\ \left. + \frac{2 \operatorname{Re} \left[\left(\frac{\alpha}{3} T_{12} + S_{12} \right) \left(\frac{\alpha}{3} T_{23} + S_{23} \right) \left(\frac{\alpha}{3} T_{31} + S_{31} \right) \right]}{W_1^+(p_1) W_1^+(p_2) W_1^+(p_3)} \right\}, \quad (67c)$$

where the ratio of the generic pion number and the total pion number ϵ is

$$\epsilon = \frac{S_{11}}{\frac{\alpha}{3} T_{11} + S_{11}}. \quad (68)$$

We assume that ϵ is independent of p . The chaoticity and weight factor are obtained as

$$\lambda_{++} = \frac{\alpha}{\alpha + \frac{6}{5} (1-\epsilon)^2}, \quad (69)$$

$$\omega_{+++} = \frac{\alpha^2 + \frac{6}{5} \alpha (1-\epsilon)^2 + \frac{27}{175} (1-\epsilon)^3 (13-28\epsilon)}{\alpha^2 + \frac{18}{5} \alpha (1-\epsilon)^2 + \frac{54}{35} (1-\epsilon)^3} \\ \times \sqrt{\frac{\frac{6}{5} (1-\epsilon)^2}{\alpha}}. \quad (70)$$

In Figs. 6 and 7, the chaoticity and weight factor are shown as functions of the mean number of DCC domains, $\langle N \rangle = \alpha$, for various values of ϵ .

The chaoticity and weight factor of neutral pions are obtained as

$$\lambda_{00} = \frac{\alpha}{\alpha + \frac{9}{5} (1-\epsilon)^2}, \quad (71)$$

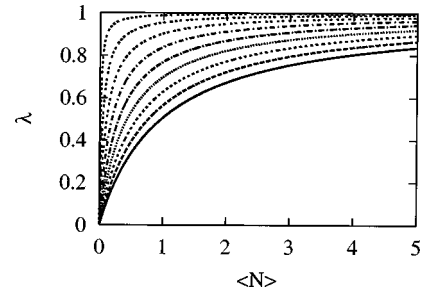


FIG. 6. Chaoticity λ of the positive pions for the model of multiple DCC domains with one chaotic generic source, as a function of the mean number of DCC domains $\langle N \rangle$. The curves are shown for the ratio of the generic pion number and the total pion number, $\epsilon = 0.1 - 0.9$, with step 0.1 from down to up.

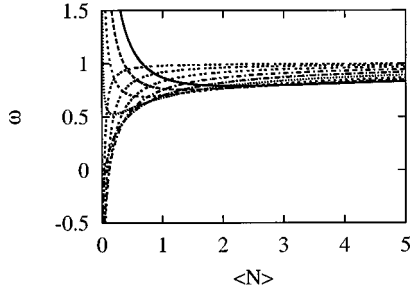


FIG. 7. Weight factor ω of the positive pions for the model of multiple DCC domains with one chaotic generic source (M-DCC/G), as a function of the mean number of DCC domains $\langle N \rangle$ varying the ratio of the generic pion number and the total pion number ϵ from 0.1 to 0.9 with step 0.1, from down to up at $\langle N \rangle = 5$.

$$\omega_{000} = \frac{1}{2} \frac{2\alpha^2 + \frac{18}{5}\alpha(1-\epsilon)^2 + \frac{81}{175}(1-\epsilon)^3(17-42\epsilon)}{\alpha^2 + \frac{27}{5}\alpha(1-\epsilon)^2 + \frac{27}{7}(1-\epsilon)^3} \times \sqrt{\frac{\alpha + \frac{9}{5}(1-\epsilon)^3}{\alpha}}, \quad (72)$$

where the spectra of neutral generic pions is the same as that of the positive ones, or $S_{11}^+ = S_{11}^0$. The correlation functions of nonidentical pions have no HBT effect, as in the two previous models.

If N DCC domains are produced, the fractional neutral-pion number is actually

$$f = \frac{\sum_n^N f_n T_{11} + S_{11}^0}{NT_{11} + S_{11}^0 + S_{11}^+ + S_{11}^-} = \frac{\sum_n^N 3f_n(1-\epsilon) + \epsilon\alpha}{3N(1-\epsilon) + 3\epsilon\alpha}. \quad (73)$$

As a consequence, the probability distribution of f is

$$P_{\alpha,\epsilon}(f) = \sum_{N=0}^{\infty} \frac{\alpha^N}{N!} e^{-\alpha} \times \int \delta\left(f - \frac{\sum_n^N 3f_n(1-\epsilon) + \epsilon\alpha}{3N(1-\epsilon) + 3\epsilon\alpha}\right) \prod_{n=1}^N \frac{df_n}{2\sqrt{f_n}}. \quad (74)$$

V. DISCUSSIONS AND SUMMARY

As we have seen in Sec. III, the pions emitted from a single coherent source of a DCC do not yield pion interferometry useful for identifying a signature of the DCC. Also, when the pions are emitted from a source in which a single coherent DCC source and a chaotic source are combined, this situation remains practically the same. Figures 1 and 3 show that the partially coherent DCC source (PC-DCC) and the partially coherent generic source (PC-G) each yield a chaoticity and weight factor similar to that of the other. The difference between the two is numerically too close for interferometry to serve as a means identifying a DCC signature.

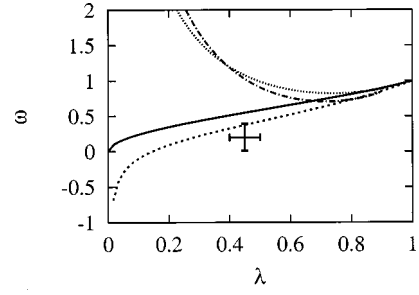


FIG. 8. Weight factor as a function of chaoticity for the positive pions. The solid and dashed curves represent the partially coherent generic model (PC-G) and the partially coherent DCC model (PC-DCC). The dotted and dot-dashed curves represent the multiple coherent generic model (M-G) and the multiple DCC domain model (M-DCC), respectively. The data point is that from the CERN NA44 [7].

If pion interferometry for the neutral pions should become feasible, combined data of charged and neutral-pion interferometry would serve as a means. Note that the pion interferometry of different charges exhibits no HBT effect and is not useful.

Figure 8 illustrates the weight factor as a function of the chaoticity in the models examined in this work, except for the model of multiple DCC domains with one generic source (M-DCC/G). For comparison, we also show in this figure the recent experimental data from the CERN NA44 Collaboration [7], the chaoticity and weight factor being $0.4-0.5$ and 0.20 ± 0.19 , respectively. (We have combined the systematic and statistical uncertainties quadratically.) The partially coherent DCC model (PC-DCC) is closest to the data point, while the partially coherent generic model (PC-G) is next. The ratio ϵ of the generic pion number and the total pion number that yields the closest PC-DCC is found from Fig. 2 to be about 0.30. That is, about 70% of pions are emitted from the DCC domains. This implies that we have a large charge fluctuation of the pions emitted. Such a large charge fluctuation does not seem to have been observed in the experiments [4], however. Note that the essential aspect of the model that yields the results close to the data is the inclusion of a chaotic generic source. In Fig. 8, we see the model of multiple DCC domains (M-DCC) with no chaotic generic source yielding the weight factor far away from the data point.

Figure 9 shows that the multiple DCC domain model (M-DCC/G) successfully yields the chaoticity and weight factor in agreement with the data. The parameter values for the best fit are found to be $\alpha = \langle N \rangle = 0.18$ and $\epsilon = 0.57$ from Fig. 7. This implies that the mean number of the DCC domains is 0.18 and that the ratio of the generic pion number and the total pion number is 0.57. For these parameter values, the charge distribution, Eq. (74), is

$$P_{\alpha,\epsilon}(f) \approx 0.83P_0(f) + 0.15P_1(f). \quad (75)$$

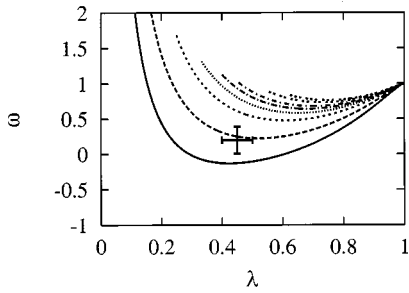


FIG. 9. Weight factor ω as a function of chaoticity λ for the positive pions, for the model of multiple DCC domains with one generic chaotic source (M-DCC/G), varying ϵ from 0 to 1. The lines from down to up correspond to the mean number of domains, $\langle N \rangle = 0.1, 0.2, 0.4, 0.6, 0.8, 1.0, 1.5,$ and 2.0 , respectively. The data is from the NA44 experiment [7].

Here, $P_0(f)$ is equal to $\delta(f - 1/3)$ in our simple model, while $P_1(f)$ is approximately the inverse square root of f , as in Eq. (1). Since $P_1(f)$ is suppressed by the factor of 0.15, $P_{\alpha,\epsilon}(f)$ of Eq. (75) is a distribution dominated by a sharp peak with a slow-varying $1/\sqrt{f}$ -like background. In practice, the sharp peak can be replaced by a smoother function, such as a binomial distribution peaking at $f = 1/3$.

We have thus shown that the NA44 data can be explained by the model of a multiple DCC model with a chaotic generic source. We have not demonstrated, however, that the NA44 data prove the appearance of the DCC. Unfortunately, if we limit ourselves to pion interferometry, we require interferometry of the neutral pions in order to strengthen the case. For the above parameter values, the chaoticity and weight factor for the neutral pions are $\lambda_{00} = 0.35$ and $\omega_{000} = -0.12$, respectively. If interferometry for the neutral pions should be carried out, these values should signal the observation of the DCC. Note that pion interferometry of differ-

ently charged pions does not serve for identifying the DCC because the generic part exhibits no HBT effect and the multiple DCC part also has no HBT effect due to the azimuthal average in isospin space (as discussed in the case of the partially coherent DCC model in Sec. IV A and in the case of the multiple DCC domain model in Sec. IV B).

A chaoticity is known to be reduced owing to decays of long-lived resonances, by an amount depending on the detector acceptance [18]. The chaoticity observed by the NA44 experiment may be affected by the resonances, and if it is substantial, our numerical analysis in the above paragraph has to be changed. Note, however, that the source model used in this work is too simple to accommodate the effect in the present form.

In summary, we have investigated two- and three-pion correlations when the DCC occurs. A chaoticity and weight factor are used as measures of two- and three-pion correlations and the various models for the DCC have been investigated. The chaoticities and weight factors for the DCC are different from the generic case. The existing experimental data are in agreement with the model of multiple DCC domains with one generic source. We suggest that the chaoticity and weight factor for neutral pions together with those for the charged pions should enable the identification occurrences of the DCC.

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